

PRACTICE PROBLEM SET 26

Calculate the volumes below. The answers are in Chapter 21.

1. Find the volume of the solid that results when the region bounded by $y = \sqrt{9 - x^2}$ and the x -axis is revolved around the x -axis.
2. Find the volume of the solid that results when the region bounded by $y = \sec x$ and the x -axis from $x = -\frac{\pi}{4}$ to $x = \frac{\pi}{4}$ is revolved around the x -axis.
3. Find the volume of the solid that results when the region bounded by $x = 1 - y^2$ and the y -axis is revolved around the y -axis.
4. Find the volume of the solid that results when the region bounded by $x = \sqrt{5}y^2$ and the y -axis from $y = -1$ to $y = 1$ is revolved around the y -axis.
5. Find the volume of the solid that results when the region bounded by $y = x^3$, $x = 2$, and the x -axis is revolved around the line $x = 2$.
6. Use the method of cylindrical shells to find the volume of the solid that results when the region bounded by $y = x$, $x = 2$, and $y = -\frac{x}{2}$ is revolved around the y -axis.
7. Use the method of cylindrical shells to find the volume of the solid that results when the region bounded by $y = \sqrt{x}$, $y = 2x - 1$, and $x = 0$ is revolved around the y -axis.
8. Use the method of cylindrical shells to find the volume of the solid that results when the region bounded by $y = x^2$, $y = 4$, and $x = 0$ is revolved around the x -axis.
9. Use the method of cylindrical shells to find the volume of the solid that results when the region bounded by $y = 2\sqrt{x}$, $x = 4$, and $y = 0$ is revolved around the y -axis.
10. Use the method of cylindrical shells to find the volume of the solid that results when the region bounded by $y^2 = 8x$ and $x = 2$ is revolved around the line $x = 4$.
11. Find the volume of the solid whose base is the region between the semi-circle $y = \sqrt{16 - x^2}$ and the x -axis, and whose cross-sections perpendicular to the x -axis are squares with a side on the base.
12. Find the volume of the solid whose base is the region between $y = x^2$ and $y = 4$ and whose perpendicular cross-sections are isosceles right triangles with the hypotenuse on the base.